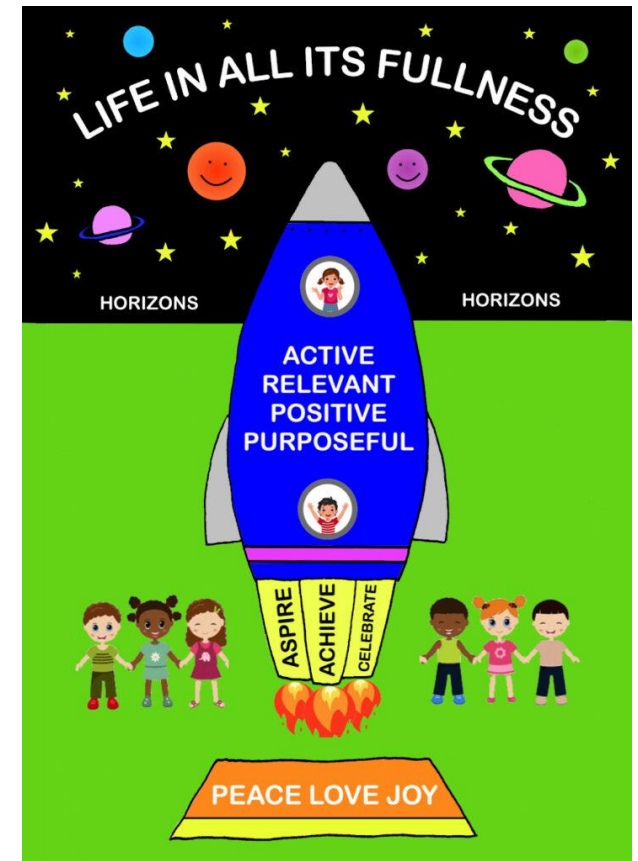




Stratford-sub-Castle CE (VC) Primary School

Calculation Progression

| | |
|---------------------------------------|--|
| Subject Leader | Miss Hannah Crook |
| Head Teacher: | Mrs Justine Watkins |
| Review Date: | July 2024 |
| To be read in conjunction with | Maths Vocabulary Progression Maths Knowledge and Skills Progression Maths 'How to' guide Maths Long Term Plan National Curriculum Unit plans & knowledge organisers |



Stratford-sub-Castle Church of England VC Primary School

Calculation Progression

Introduction

The following calculation progression has been updated to link to the *White Rose Scheme of Work* that Stratford-sub-Castle Primary School has been following since September 2017. This *White Rose Calculation Policy* has been used as a basis for this calculation progression.

Mastery Teaching Approach

At Stratford-sub-Castle CE Primary School we use a mastery teaching approach to teaching to Mathematics which follows the 'Five Big Ideas in Teaching for Mastery'.

ncetm - <https://www.ncetm.org.uk/resources/50042>

Concrete Pictorial Abstract (CPA) Approach

An essential part of teaching for mastery is the CPA Approach (concrete, pictorial, abstract). The calculation progression focuses on the links between, and also the progression through, Concrete, Pictorial and Abstract. Teachers go between the three different stages to reinforce concepts.

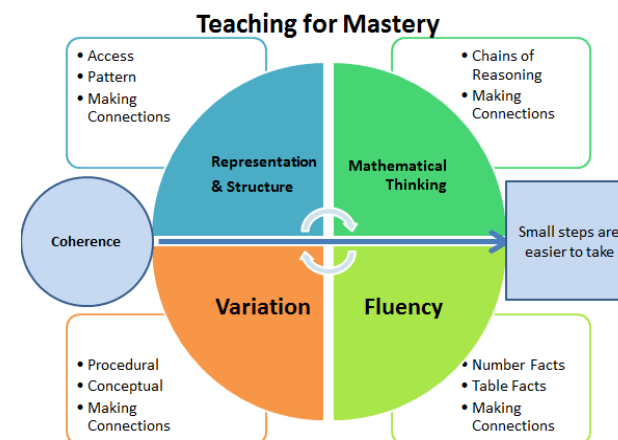
Concrete is the 'active' stage, using concrete objects/manipulatives to solve problems. Manipulatives are chosen for the pupils by the teacher. Manipulatives are selected upon the most appropriate for the concept. Teachers may vary which manipulatives are used for a concept.

Pictorial is the 'seeing' stage, using representations of the objects involved in maths problems. This stage encourages children to make a mental connection between the physical object and abstract levels of understanding, by drawing or looking at pictures, circles, diagrams or models which represent the objects in the problem.

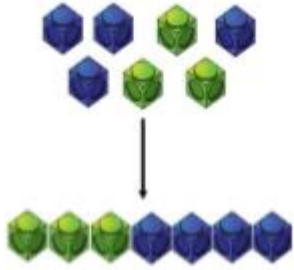
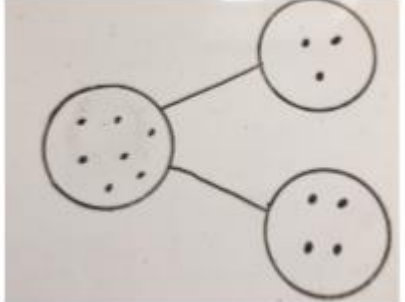
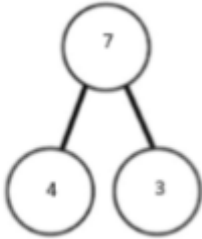
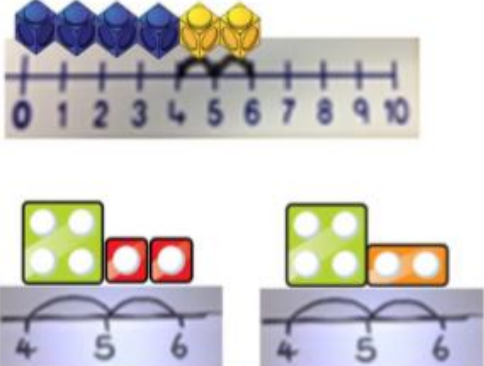
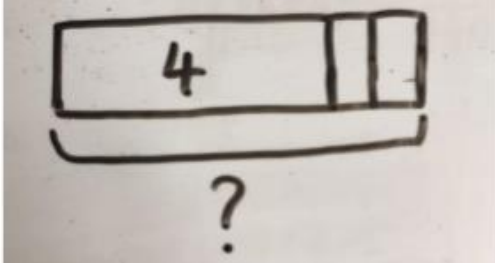
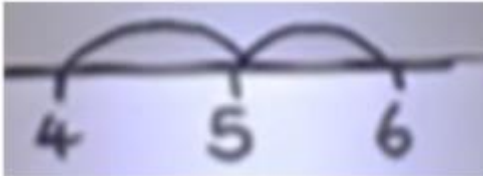
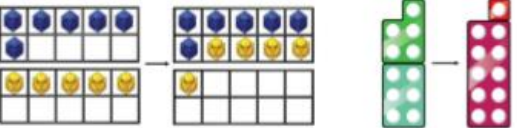
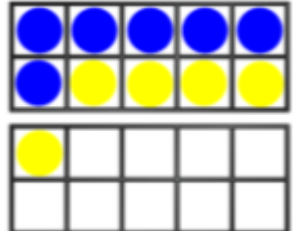
Abstract is the 'symbolic' stage, where children are able to use abstract symbols to model and solve maths problems. The 'abstract' concept is introduced when children has a firm understanding of the 'concrete' and 'pictorial'.

Language

The calculation progression also includes vocabulary and stem sentences pupils are expected to use. This is to help reinforce concepts being learnt to result in greater understanding.



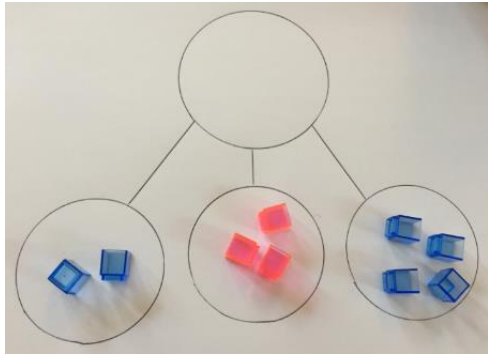
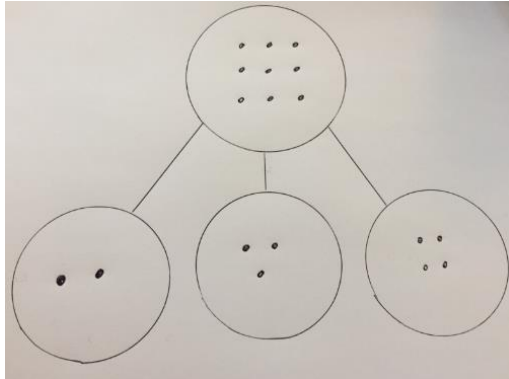
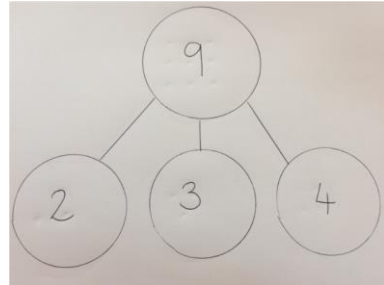
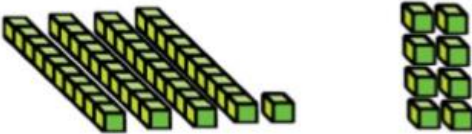
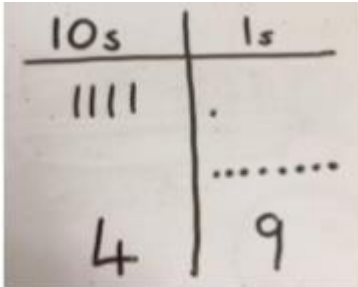
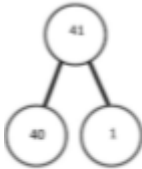
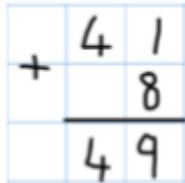
YEAR 1 – ADDITION

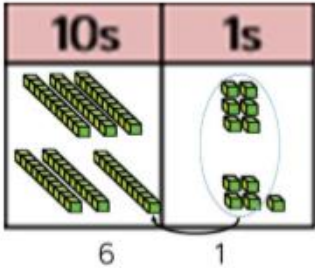
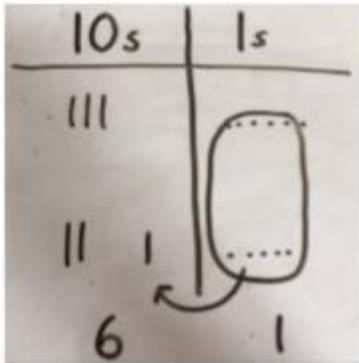
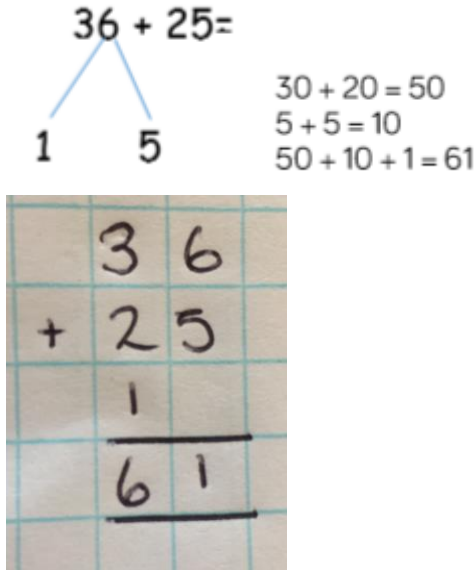
| | CONCRETE | PICTORIAL | ABSTRACT |
|---|---|---|---|
| <p>Combining two parts to make a whole</p> | <p>Use a range of manipulatives (e.g. cubes, shells, teddy bears)</p>  | <p>Children to represent the cubes using dots or crosses. They could put each part on a part whole model too</p>  | <p>$4 + 3 = 7$. Four is a part, three is a part and the whole is seven.</p>  |
| <p>Counting on using number lines</p> | <p>Using cubes or Numicon</p>  | <p>A bar model which encourages the children to count on, rather than count all.</p>  | <p>The abstract number line:</p> <p>What is 2 more than 4? What is the sum of 2 and 4? What is the total of 4 and 2? $4 + 2$</p>  |
| <p>Regrouping to make 10</p> | <p>Using tens frames and counters/ cubes or using Numicon</p> <p>$6 + 5$</p>  | <p>Children to draw the ten frame and counters/cubes.</p>  | <p>Children to develop and understanding of equality.</p> <p>$6 + \square = 11$ $6 + 5 = 5 + \square$ $6 + 5 = \square + 4$</p> |

YEAR 1 – ADDITION

| VOCABULARY <i>(new vocab in bold/italic)</i> | | | | | | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|---|--------------|--------------|-------------------|-------------|-----------------|---|
| <i>part</i> | <i>whole</i> | <i>total</i> | <i>sum</i> | <i>add</i> | <i>counting</i> | <p><i>The whole is _____ so a part is _____ and a part is _____ (The whole is 10 so a part is 6 and a part is 4)</i></p> <p><i>A part is _____ and a part is _____ so the whole is _____ (A part is 7 and a part is 3 so the whole is 10)</i></p> <p><i>The total of _____ and _____ is _____ (The total of 6 and 4 is 10).</i></p> |
| <i>tens</i> | <i>ones</i> | <i>equal</i> | <i>same value</i> | <i>plus</i> | | |
| <i>more than</i> | | | | | | |

YEAR 2 – ADDITION

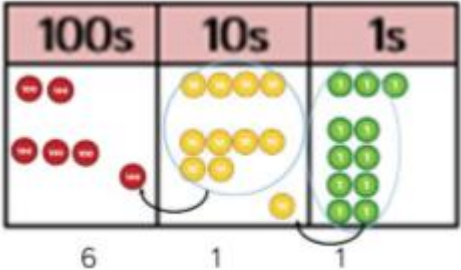
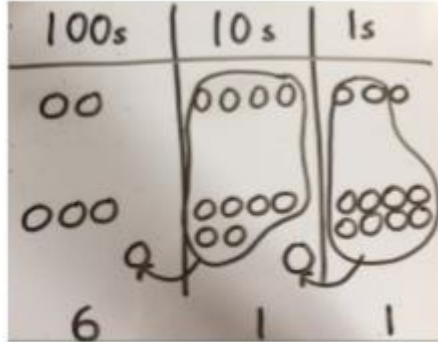
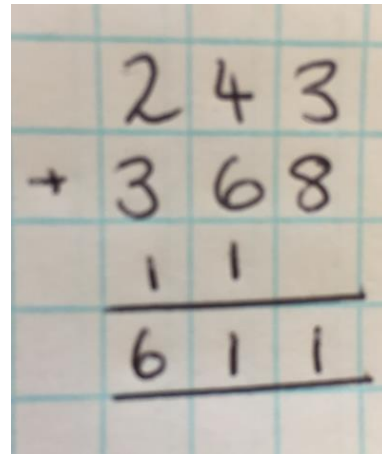
| | CONCRETE | PICTORIAL | ABSTRACT | | | | | | |
|---|---|---|---|---|--|--|---|---|---|
| <p>Adding 3 single digit numbers</p> | <p>Using manipulatives</p>  | <p>Children to represent the cubes using dots or crosses. They could put each part on a part whole model too</p>  | <p>$2 + 3 + 4 = 9$. Four is a part, three is a part, two is a part and the whole is nine.</p>  <table border="1" style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <tr> <td colspan="3" style="text-align: center; padding: 5px;">9</td> </tr> <tr> <td style="text-align: center; padding: 5px;">2</td> <td style="text-align: center; padding: 5px;">3</td> <td style="text-align: center; padding: 5px;">4</td> </tr> </table> | 9 | | | 2 | 3 | 4 |
| 9 | | | | | | | | | |
| 2 | 3 | 4 | | | | | | | |
| <p>TO + O using base 10.</p> | <p>Continue to develop understanding of partitioning and place value $41 + 8$</p>  | <p>Children to represent the base 10 (e.g. lines of tens and dot/crosses for ones).</p>  | <p>$41 + 8$</p>  <p style="margin-left: 20px;">$1 + 8 = 9$ $40 + 9 = 49$</p>  | | | | | | |

| | CONCRETE | PICTORIAL | ABSTRACT |
|-------------------------------|--|---|--|
| TO + TO using base 10. | Continue to develop understanding of partitioning and place value. $36 + 25$  | Children to represent the base 10 in a place value chart.  | Looking for ways to make 10. $36 + 25 =$  |

YEAR 2 – ADDITION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|--|---|
| part whole total sum add counting tens ones equal same value plus more than | The whole is _____ so a part is _____ and a part is _____ (The whole is 10 so a part is 6 and a part is 4) A part is _____ and a part is _____ so the whole is _____ (A part is 7 and a part is 3 so the whole is 10) The total of _____ and _____ is _____ (The total of 6 and 4 is 10). The sum of _____ and _____ is _____ (The sum of 6 and 4 is 10). |

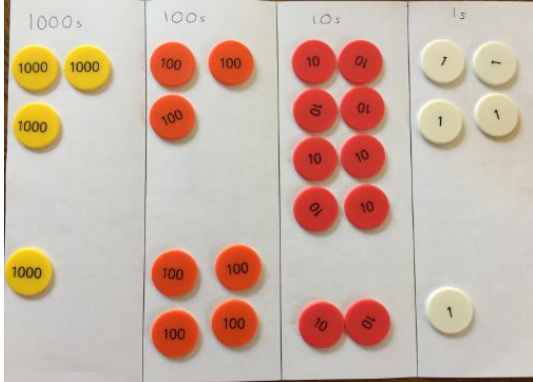
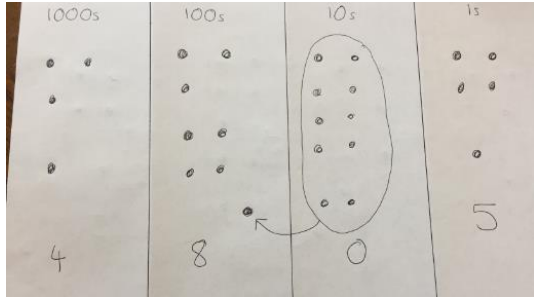
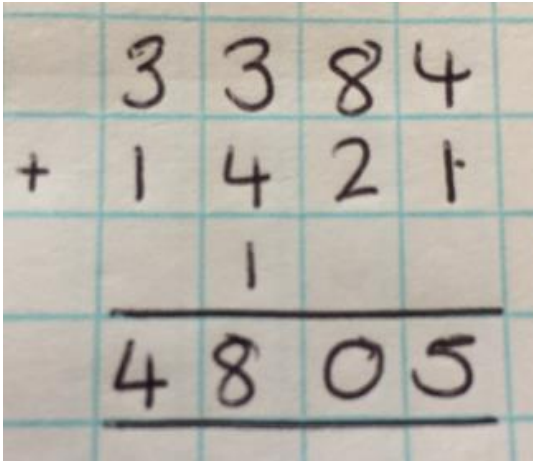
YEAR 3 – ADDITION

| | CONCRETE | PICTORIAL | ABSTRACT |
|--|---|---|--|
| <p>Use of place value counters to add HTO + TO, HTO + HTO etc</p> | <p>When there are 10 ones in the 1s column – we exchange for 1 ten; when there are 10 tens in the 10s column – we exchange for 1 hundred.</p>  | <p>Children to represent the counters in a place value chart, circling when they make an exchange.</p>  | <p>Formal method</p>  |

YEAR 3 – ADDITION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> | | | | | | | | | | | | | | | | | | |
|--|---|-----------------|------------|------|----------|----------|------|------|-------|------------|------|----------|-----------|---------------|-----------------|--|--|--|---|
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| part | whole | total | sum | add | counting | | | | | | | | | | | | | | |
| tens | ones | equal | same value | plus | exchange | | | | | | | | | | | | | | |
| more than | column | hundreds | | | | | | | | | | | | | | | | | |

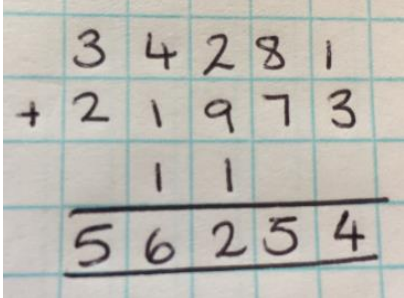
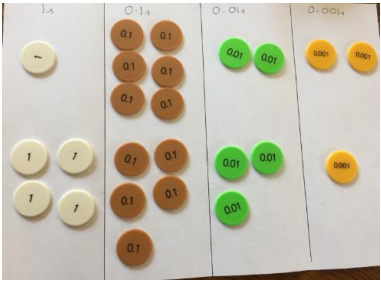
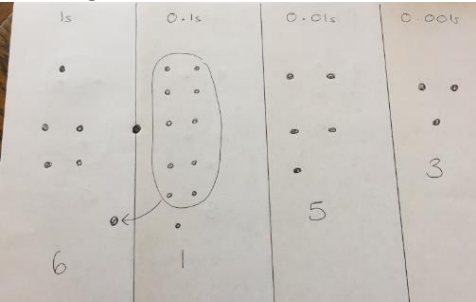
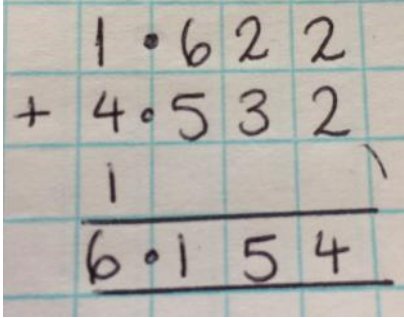
YEAR 4 – ADDITION

| | CONCRETE | PICTORIAL | ABSTRACT |
|---|---|---|--|
| <p>Use of place value counters to add ThHTO + TO, ThHTO + HTO, ThHTO + ThHTO etc</p> | <p>When there are 10 ones in the 1s column – we exchange for 1 ten; when there are 10 tens in the 10s column – we exchange for 1 hundred; when there are 10 hundreds in the 100s column – we exchange for 1 thousand.</p>  | <p>Children to represent the counters in a place value chart, circling when they make an exchange.</p>  | <p>Formal method</p>  |

YEAR 4 – ADDITION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|--|---|
| <p>part whole total sum add</p> <p>tens ones equal same value</p> <p>more than column hundreds</p> <p><i>thousands</i></p> | <p>The whole is _____ so a part is _____ and a part is _____ (The whole is 10 so a part is 6 and a part is 4)</p> <p>A part is _____ and a part is _____ so the whole is _____ (A part is 7 and a part is 3 so the whole is 10)</p> <p>The total of _____ and _____ is _____ (The total of 6 and 4 is 10).</p> <p>The sum of _____ and _____ is _____ (The sum of 6 and 4 is 10).</p> |

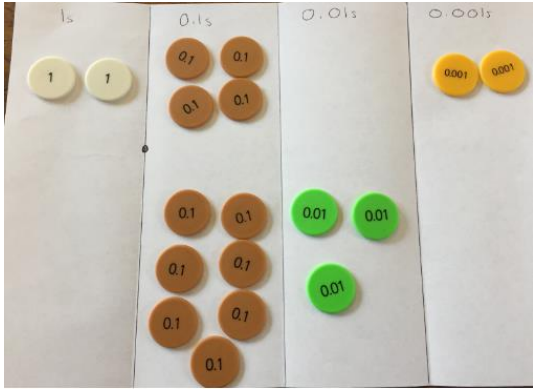
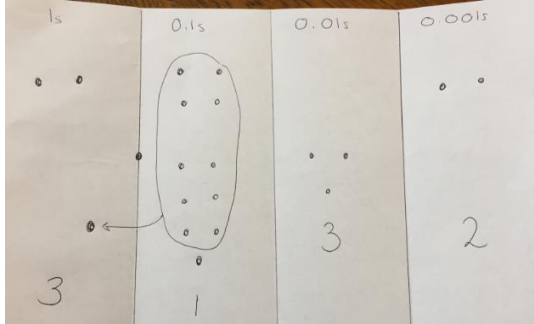
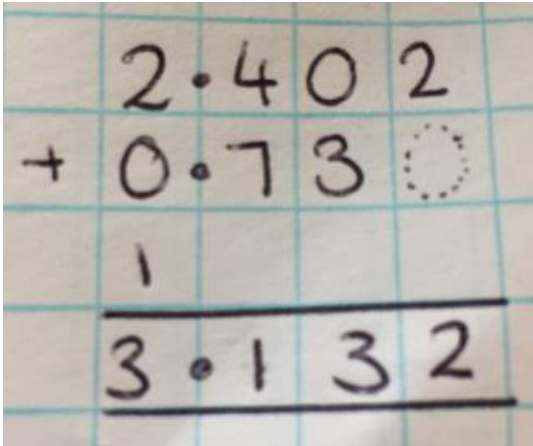
YEAR 5 – ADDITION

| | CONCRETE | PICTORIAL | ABSTRACT |
|--|---|---|--|
| Use of place value counters to add integers | | | Formal method  |
| Use of place values to add decimals up to 3 d.p (same number of decimal places). | Exchange counters for the next base 10 unit.  | Children to represent the counters in a place value chart, circling when they make an exchange.  | Formal method  |

YEAR 5 – ADDITION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|--|---|----------------|--------------|-----|------------------|----------|------|------|-------|------------|--|------|-----------|--|--------|----------|--|----------|-----------|--|----------------|--------------|--|------------------|-------------------|--|--|--|--|--|--|
| <table style="width: 100%; border: none;"> <tr> <td style="width: 12.5%;">part</td> <td style="width: 12.5%;">whole</td> <td style="width: 12.5%;">total</td> <td style="width: 12.5%;">sum</td> <td style="width: 12.5%;">add</td> <td style="width: 12.5%;">counting</td> </tr> <tr> <td>tens</td> <td>ones</td> <td>equal</td> <td>same value</td> <td></td> <td>plus</td> </tr> <tr> <td>more than</td> <td></td> <td>column</td> <td>hundreds</td> <td></td> <td>exchange</td> </tr> <tr> <td>thousands</td> <td></td> <td>decimal</td> <td>tenth</td> <td></td> <td>hundredth</td> </tr> <tr> <td>thousandth</td> <td></td> <td></td> <td></td> <td></td> <td></td> </tr> </table> | part | whole | total | sum | add | counting | tens | ones | equal | same value | | plus | more than | | column | hundreds | | exchange | thousands | | decimal | tenth | | hundredth | thousandth | | | | | | The whole is _____ so a part is _____ and a part is _____ (The whole is 10 so a part is 6 and a part is 4) A part is _____ and a part is _____ so the whole is _____ (A part is 7 and a part is 3 so the whole is 10) The total of ____ and ____ is ____ (The total of 6 and 4 is 10). The sum of ____ and ____ is ____ (The sum of 6 and 4 is 10). |
| part | whole | total | sum | add | counting | | | | | | | | | | | | | | | | | | | | | | | | | | |
| tens | ones | equal | same value | | plus | | | | | | | | | | | | | | | | | | | | | | | | | | |
| more than | | column | hundreds | | exchange | | | | | | | | | | | | | | | | | | | | | | | | | | |
| thousands | | decimal | tenth | | hundredth | | | | | | | | | | | | | | | | | | | | | | | | | | |
| thousandth | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

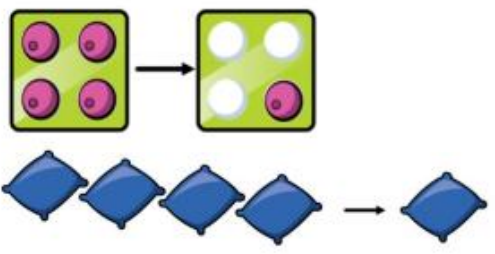
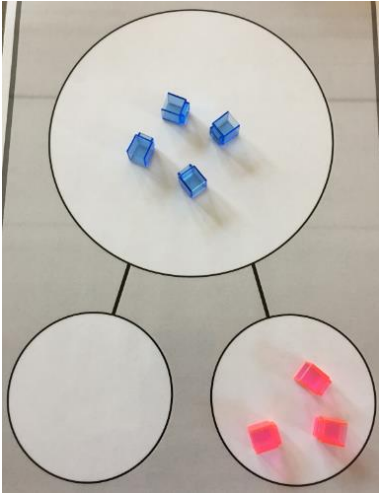
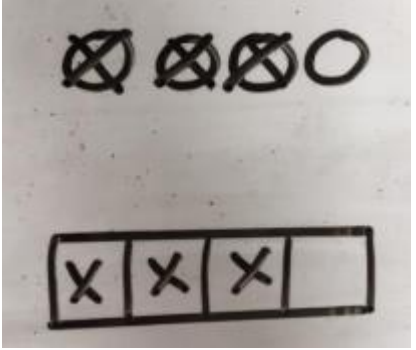
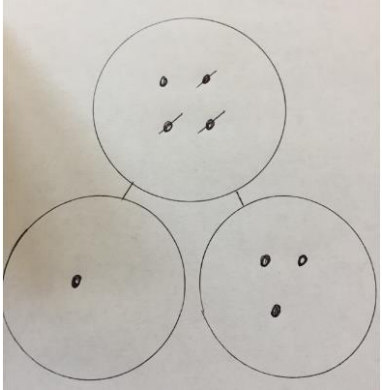

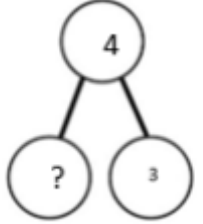
YEAR 6 – ADDITION


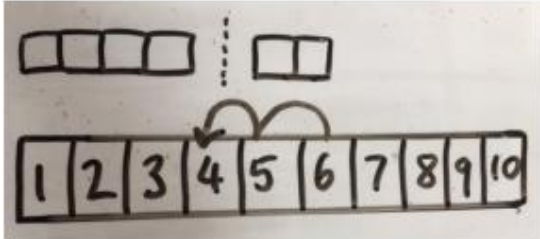
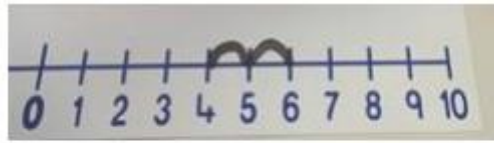
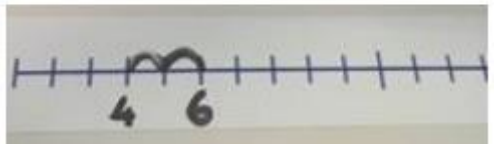
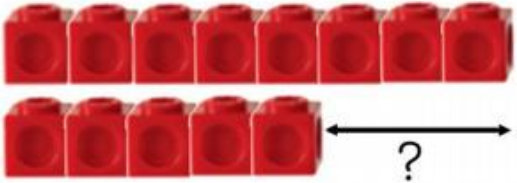
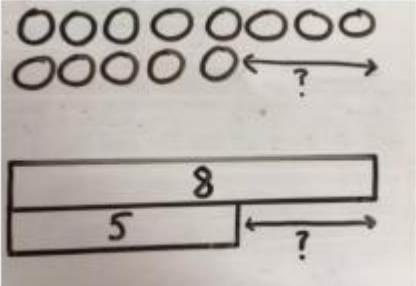
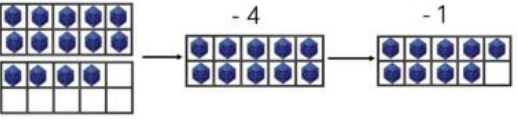
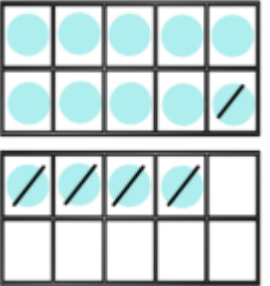
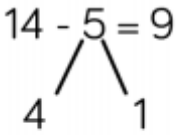
| | CONCRETE | PICTORIAL | ABSTRACT |
|--|---|---|--|
| <p>Use of place values to add decimals up to 3 d.p (different number of decimal places.</p> | <p>Exchange counters for the next base 10 unit.</p>  | <p>Children to represent the counters in a place value chart, circling when they make an exchange.</p>  | <p>Formal method</p>  |

YEAR 6 – ADDITION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|--|---|----------|------------|-----------|----------|----------|------|------|-------|------------|------|----------|-----------|--------|----------|-------|-----------|--|-----------|---------|--|--|--|--|------------|--|--|--|--|--|---|
| <table style="width: 100%; border: none;"> <tr> <td style="padding: 5px;">part</td> <td style="padding: 5px;">whole</td> <td style="padding: 5px;">total</td> <td style="padding: 5px;">sum</td> <td style="padding: 5px;">add</td> <td style="padding: 5px;">counting</td> </tr> <tr> <td style="padding: 5px;">tens</td> <td style="padding: 5px;">ones</td> <td style="padding: 5px;">equal</td> <td style="padding: 5px;">same value</td> <td style="padding: 5px;">plus</td> <td style="padding: 5px;">exchange</td> </tr> <tr> <td style="padding: 5px;">more than</td> <td style="padding: 5px;">column</td> <td style="padding: 5px;">hundreds</td> <td style="padding: 5px;">tenth</td> <td style="padding: 5px;">hundredth</td> <td style="padding: 5px;"></td> </tr> <tr> <td style="padding: 5px;">thousands</td> <td style="padding: 5px;">decimal</td> <td style="padding: 5px;"></td> <td style="padding: 5px;"></td> <td style="padding: 5px;"></td> <td style="padding: 5px;"></td> </tr> <tr> <td style="padding: 5px;">thousandth</td> <td style="padding: 5px;"></td> <td style="padding: 5px;"></td> <td style="padding: 5px;"></td> <td style="padding: 5px;"></td> <td style="padding: 5px;"></td> </tr> </table> | part | whole | total | sum | add | counting | tens | ones | equal | same value | plus | exchange | more than | column | hundreds | tenth | hundredth | | thousands | decimal | | | | | thousandth | | | | | | <p>The whole is _____ so a part is _____ and a part is _____ (The whole is 10 so a part is 6 and a part is 4)</p> <p>A part is _____ and a part is _____ so the whole is _____ (A part is 7 and a part is 3 so the whole is 10)</p> <p>The total of ____ and ____ is _____. (The total of 6 and 4 is 10).</p> <p>The sum of ____ and ____ is _____. (The sum of 6 and 4 is 10).</p> |
| part | whole | total | sum | add | counting | | | | | | | | | | | | | | | | | | | | | | | | | | |
| tens | ones | equal | same value | plus | exchange | | | | | | | | | | | | | | | | | | | | | | | | | | |
| more than | column | hundreds | tenth | hundredth | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| thousands | decimal | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| thousandth | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

YEAR 1 – SUBTRACTION



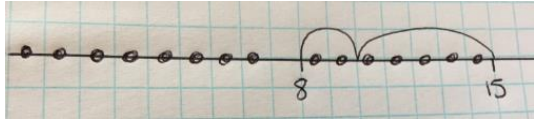
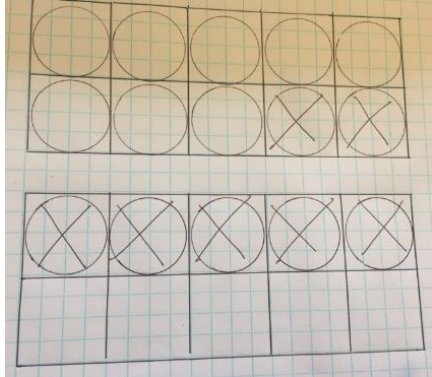
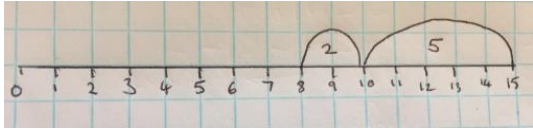
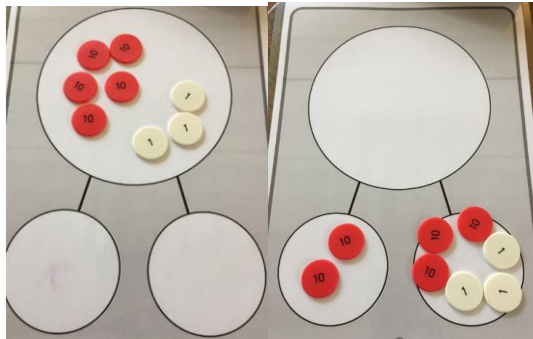
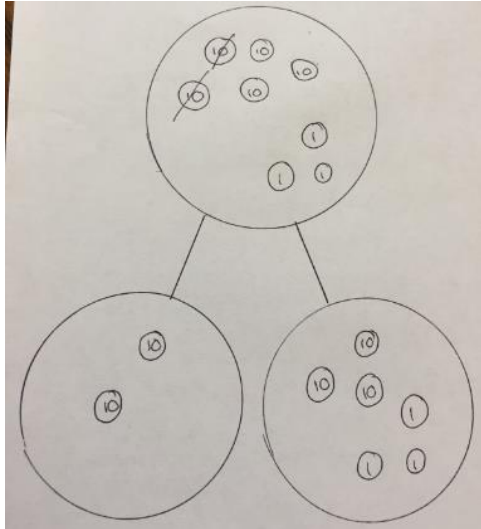
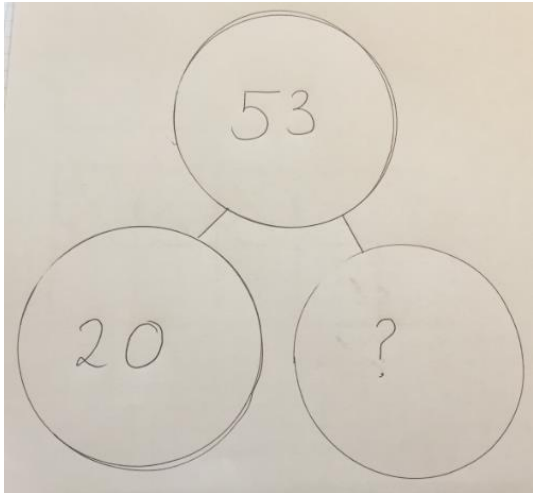
| | CONCRETE | PICTORIAL | ABSTRACT | | | | |
|---|--|--|--|---|--|---|---|
| <p>Physically taking away and removing objects from a whole.</p> | <p>Tens frame, Numicon, cube and other items such as bean bags could be used.</p> <p>$4 - 3 = 1$</p>   | <p>Children to draw the concrete resources they are using and cross out the correct amount. The bar model can also be used.</p>  <p>Using the part whole model –drawing dots</p>  | <p>$4 - 3 =$</p> <p> $= 4 - 3$</p> <table border="1" data-bbox="1579 343 1892 422"> <tr> <td colspan="2">4</td> </tr> <tr> <td>3</td> <td>?</td> </tr> </table>  | 4 | | 3 | ? |
| 4 | | | | | | | |
| 3 | ? | | | | | | |

| | CONCRETE | PICTORIAL | ABSTRACT |
|--------------------------------|--|--|--|
| Counting back | Using number lines or number tracks – children start with 6 and count back 2 $6 - 2 = 4$  | Children to represent what they see pictorially  | Children to represent the calculation on a number line or number track and show their jumps. Encourage children to use an empty number line.   |
| Finding the difference. | Using cubes, Numicon or Cuisinaire rods, other objects can also be used. Calculate the difference between 8 and 5.  | Children to draw the cubes/ other concrete objects which they have used or the bar model to illustrate that they need to calculate.  | Find the difference between 8 and 5. $8 - 5$, the difference is <input type="text"/> Children to explore why $9 - 6 = 8 - 5 = 7 - 4$ have the same difference. |
| Making 10 | Using ten frames $14 - 5$  | Children to present the ten frame pictorially and discuss what they did to make 10.  | Children to show how they can make 10 by partitioning the subtrahend. $14 - 5 = 9$  $14 - 4 = 10$ $10 - 1 = 9$ |

YEAR 1 – SUBTRACTION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|--|--|
| <p style="text-align: center;"><i>take away</i> <i>less than</i> <i>the difference</i> <i>subtract</i></p> <p style="text-align: center;"><i>minus</i> <i>fewer</i> <i>decrease</i></p> | <p>The whole is _____ so a part is _____ and a part is _____ (The whole is 10 so a part is 6 and a part is 4)</p> <p>A part is _____ and a part is _____ so the whole is _____ (A part is 7 and a part is 3 so the whole is 10)</p> <p><i>The difference between _____ and _____ is _____ (The difference between 12 and 4 is 8).</i></p> |

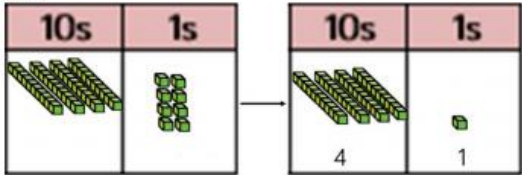
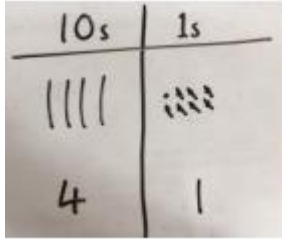
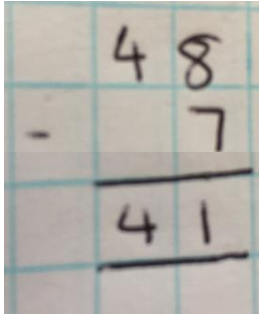
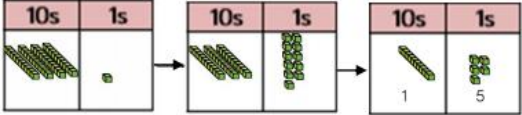
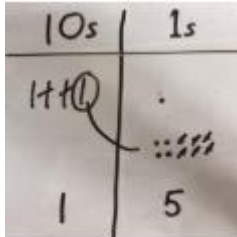
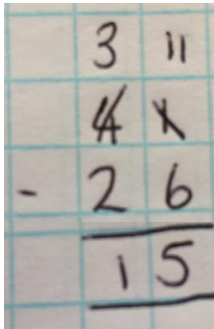
YEAR 2 – SUBTRACTION

| | CONCRETE | PICTORIAL | ABSTRACT |
|----------------------|--|--|--|
| 2-digit – 1s | <p>Using a bead string</p>  <p>Tens frame</p>  | <p>Bead string drawing</p>  <p>Tens frame – cross out</p>  | <p>Number line</p>  |
| 2-digit – 10s | <p>Using dienes or place value counters</p>  | <p>Using place value grid with circles labelled with units</p>  | <p>Using part whole model</p>  |

YEAR 2 – SUBTRACTION

| VOCABULARY <i>(new vocab in bold/italic)</i> | | | | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|---|--|--|---|--|
| take away minus <i>tens</i> | less than decrease <i>ones</i> | the difference <i>Partitioning</i> | subtract <i>place value</i> | <p>The whole is _____ so a part is _____ and a part is _____ (The whole is 10 so a part is 6 and a part is 4)</p> <p>A part is _____ and a part is _____ so the whole is _____ (A part is 7 and a part is 3 so the whole is 10)</p> <p>The difference between _____ and _____ is _____ (The difference between 12 and 4 is 8).</p> |

YEAR 3 – SUBTRACTION


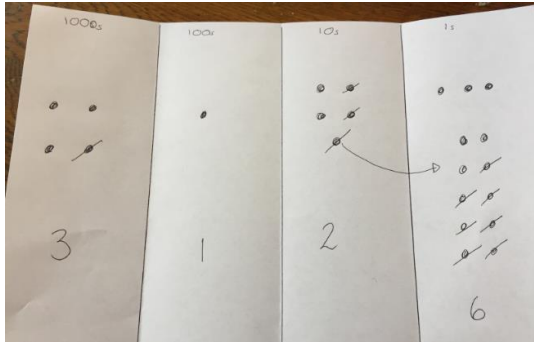
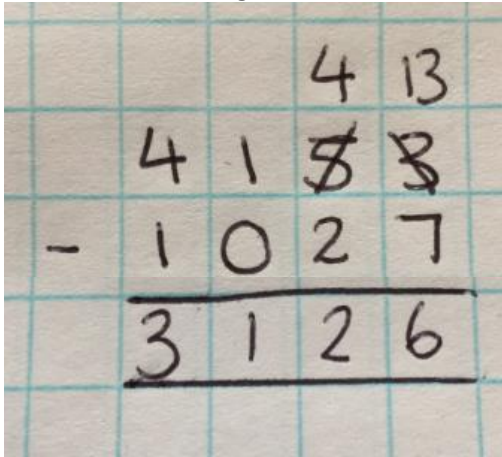
| | CONCRETE | PICTORIAL | ABSTRACT |
|---|--|--|---|
| Column method TO - O | Using base 10 $48 - 7$  | Children to represent the base 10 pictorially.  | Column method or children could count back 7.  |
| Column method TO - TO | Using base 10 and having to exchange $41 - 26$  | Represent the base 10 pictorially, remembering to show the exchange.  | Formal column method. Children must understand that when they have exchanged the 10 they still have 41 because $41 = 30 + 11$  |
| Column method HTO - TO | Using place value counters. | Represent the place value counters pictorially; remembering to show what has been exchanged. | Formal column method. Children must understand what has happened when they have crossed out digits. |

| | CONCRETE | PICTORIAL | ABSTRACT |
|--|-----------------|-----------|----------|
| | <p>234 - 88</p> | | |

YEAR 3 – SUBTRACTION

| VOCABULARY <i>(new vocab in bold/italic)</i> | | | | STEM SENTENCES <i>(new vocab in bold/italic)</i> | |
|---|-----------|----------------|-----------------|--|--|
| take away | less than | the difference | subtract | The whole is _____ so a part is _____ and a part is _____ (The whole is 10 so a part is 6 and a part is 4) | |
| minus | fewer | decrease | ones | A part is _____ and a part is _____ so the whole is _____ (A part is 7 and a part is 3 so the whole is 10) | |
| place value | tens | column | exchange | The difference between _____ and _____ is _____ (The difference between 12 and 4 is 8). | |

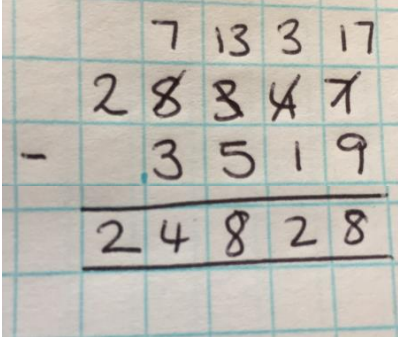
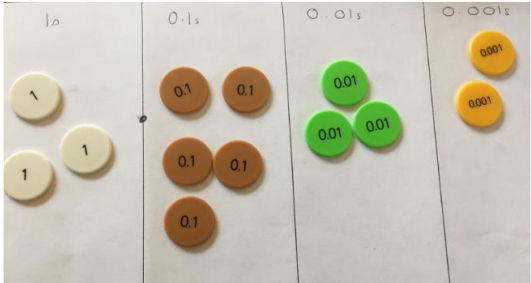
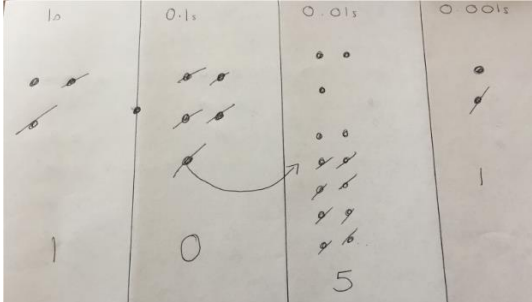
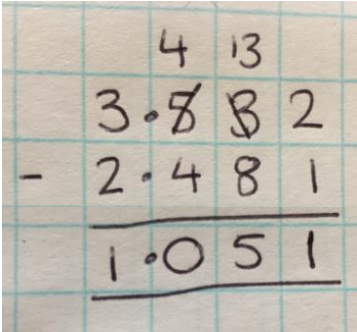
YEAR 4 – SUBTRACTION

| | CONCRETE | PICTORIAL | ABSTRACT |
|--|--|--|--|
| <p>Column method 4-digit – up to 4-digit</p> | <p>Using place value counters.</p>  | <p>Represent the place value counters pictorially; remembering to show what has been exchanged.</p>  | <p>Formal column method. Children must understand what has happened when they have crossed out digits.</p>  |

YEAR 4 – SUBTRACTION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> | | | | | | | | | | | | | | | | |
|--|---|----------------|----------------|----------|-------|-------|----------|------|-------------|------|--------------|----------|------------------|--|--------|--|--|
| <table style="width: 100%; border: none;"> <tr> <td style="width: 25%;">take away</td> <td style="width: 25%;">less than</td> <td style="width: 25%;">the difference</td> <td style="width: 25%;">subtract</td> </tr> <tr> <td>minus</td> <td>fewer</td> <td>decrease</td> <td>ones</td> </tr> <tr> <td>place value</td> <td>tens</td> <td>partitioning</td> <td>exchange</td> </tr> <tr> <td>thousands</td> <td></td> <td>column</td> <td></td> </tr> </table> | take away | less than | the difference | subtract | minus | fewer | decrease | ones | place value | tens | partitioning | exchange | thousands | | column | | <p>The whole is _____ so a part is _____ and a part is _____ (The whole is 10 so a part is 6 and a part is 4)</p> <p>A part is _____ and a part is _____ so the whole is _____ (A part is 7 and a part is 3 so the whole is 10)</p> <p>The difference between _____ and _____ is _____ (The difference between 12 and 4 is 8).</p> |
| take away | less than | the difference | subtract | | | | | | | | | | | | | | |
| minus | fewer | decrease | ones | | | | | | | | | | | | | | |
| place value | tens | partitioning | exchange | | | | | | | | | | | | | | |
| thousands | | column | | | | | | | | | | | | | | | |

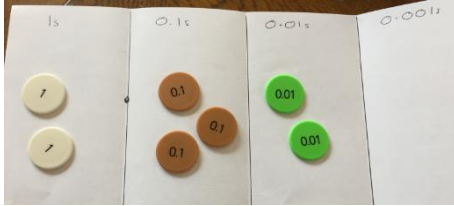
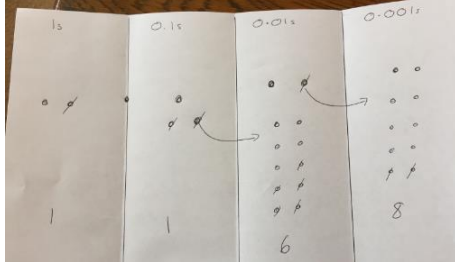
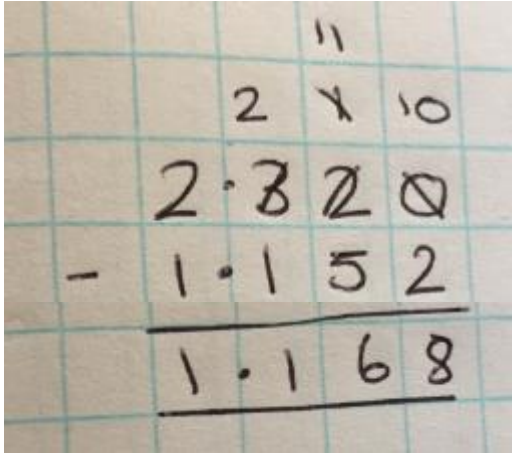
YEAR 5 – SUBTRACTION

| | CONCRETE | PICTORIAL | ABSTRACT |
|--|--|--|---|
| <p>Column method - integers</p> | | | <p>Formal column method. Children must understand what has happened when they have crossed out digits.</p>  |
| <p>Column method – decimals (same number up to 3 d.p)</p> | <p>Using place value counters</p>  | <p>Children to represent the counters in a place value chart, circling when they make an exchange.</p>  | <p>Formal column method. Children must understand what has happened when they have crossed out digits.</p>  |

YEAR 5 – SUBTRACTION

| VOCABULARY <i>(new vocab in bold/italic)</i> | | | | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|--|---|--|--|---|
| take away minus fewer place value thousands thousandth | less than decrease tens decimal | the difference partitioning column tenth | subtract Ones Exchange Hundredth | The whole is _____ so a part is _____ and a part is _____ (The whole is 10 so a part is 6 and a part is 4) A part is _____ and a part is _____ so the whole is _____ (A part is 7 and a part is 3 so the whole is 10) The difference between _____ and _____ is _____ (The difference between 12 and 4 is 8). |

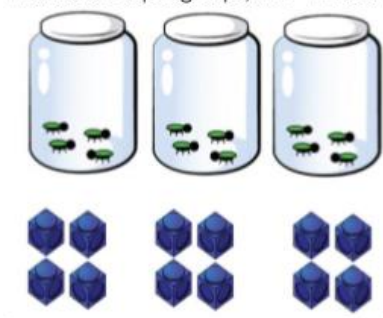
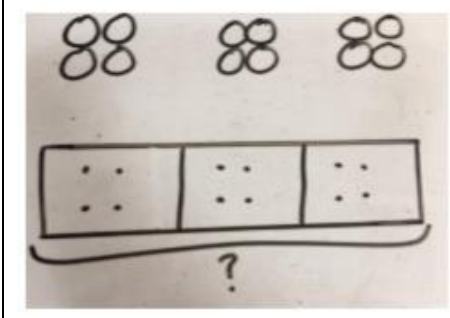

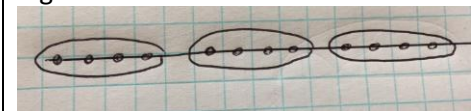
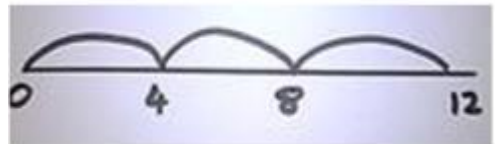
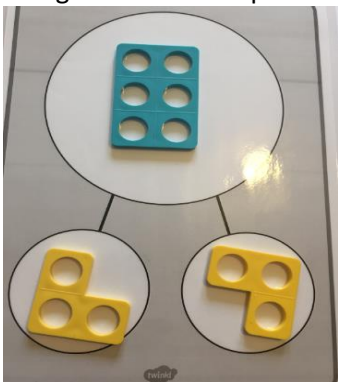
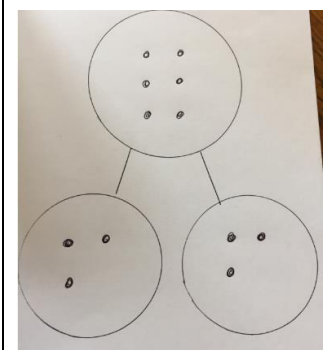
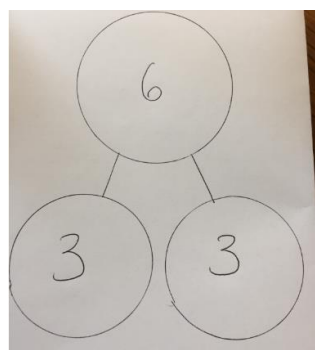
YEAR 6 – SUBTRACTION

| | CONCRETE | PICTORIAL | ABSTRACT |
|---|---|---|--|
| <p>Column method – decimals (different number up to 3 d.p)</p> | <p>Using place value counters</p>  | <p>Children to represent the counters in a place value chart, circling when they make an exchange.</p>  | <p>Formal column method. Children must understand what has happened when they have crossed out digits.</p>  |

YEAR 6 – SUBTRACTION

| VOCABULARY <i>(new vocab in bold/italic)</i> | | | | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|---|-----------|----------------|-----------|--|
| take away | less than | the difference | subtract | <p>The whole is _____ so a part is _____ and a part is _____ (The whole is 10 so a part is 6 and a part is 4)</p> <p>A part is _____ and a part is _____ so the whole is _____ (A part is 7 and a part is 3 so the whole is 10)</p> <p>The difference between _____ and _____ is _____ (The difference between 12 and 4 is 8).</p> |
| minus | fewer | decrease | ones | |
| place value | tens | partitioning | exchange | |
| thousands | decimal | column | hundredth | |
| thousandth | | tenth | | |

YEAR 1 – MULTIPLICATION

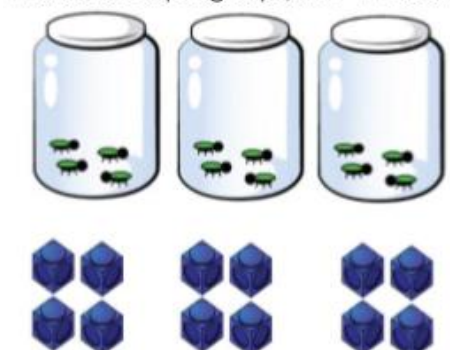
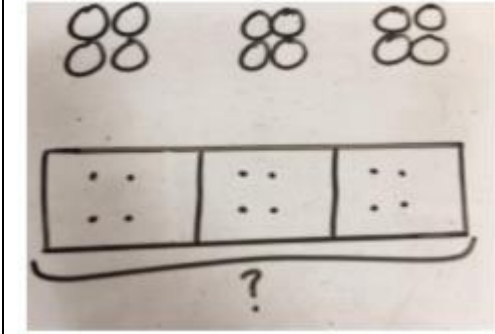

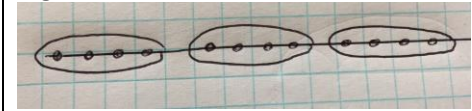
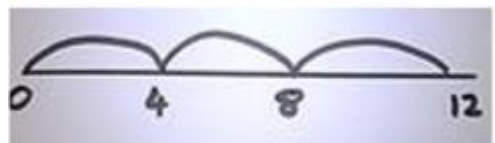
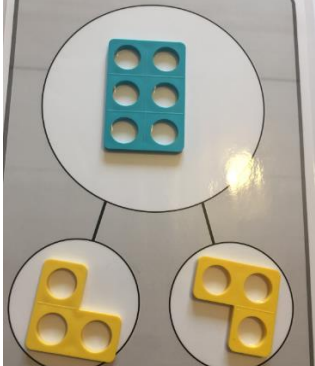
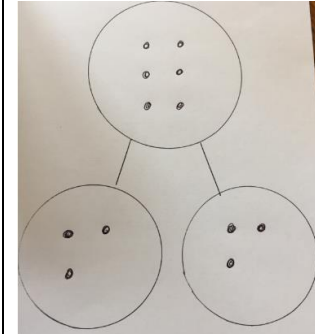
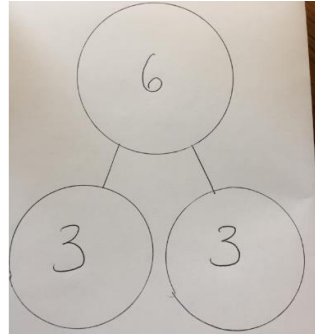
| | CONCRETE | PICTORIAL | ABSTRACT |
|---|---|---|--|
| Repeated grouping/ repeated addition | 3×4 $4 + 4 + 4$ There are 3 equal groups, with 4 in each group.  | Children to represent the practical resources in a picture and use a bar model.  | **TEACHER MODEL** Use alongside concrete/pictorial representation $3 \times 4 = 12$ $4 + 4 + 4 = 12$ |
| Numberlines to show repeated groups | Using a beadstring 3×4  | Represent this pictorially alongside a number line e.g.  | **TEACHER MODEL** Use alongside concrete/pictorial representation Abstract number line showing three jumps of four  |
| Doubling | Using Numicon with part-whole model  | Using dots with part-whole model  | Using numbers with part-whole model  |

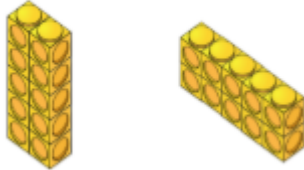
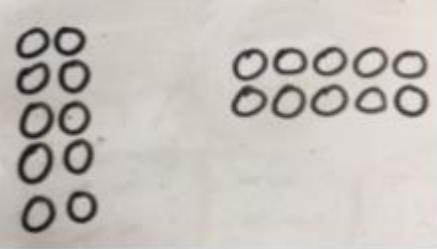
YEAR 1 – MULTIPLICATION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|--|--|
| <i>repeated addition</i> <i>multiply</i> <i>times</i> <i>grouping</i> <i>lots of</i> <i>equal groups of</i> <i>double</i> | The whole is _____ there are _____ equal parts of _____ (The whole is 24 there are 4 equal parts of 6) |

YEAR 2 – MULTIPLICATION

N.B. Similar strategies to Y1

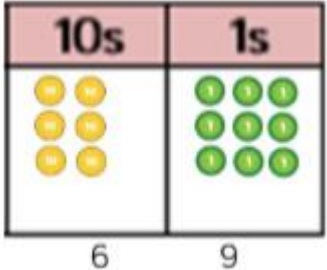
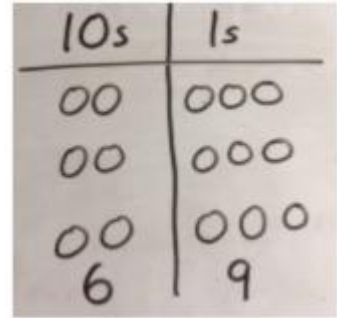
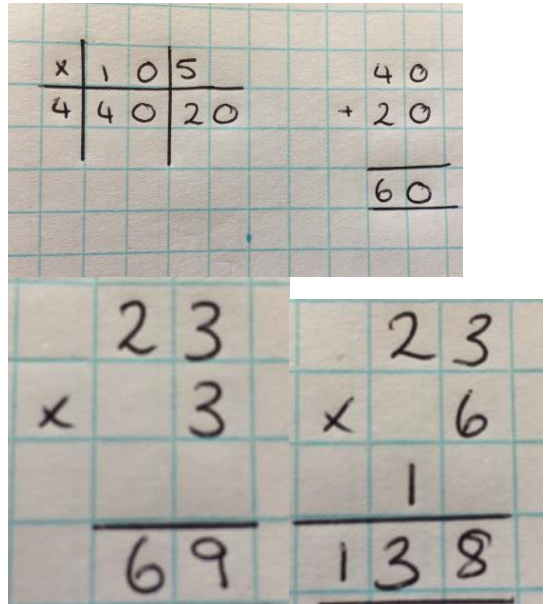
| | CONCRETE | PICTORIAL | ABSTRACT |
|---|---|---|---|
| Repeated grouping/ repeated addition | 3×4 $4 + 4 + 4$ There are 3 equal groups, with 4 in each group.  | Children to represent the practical resources in a picture and use a bar model.  | Use alongside concrete/pictorial representation $3 \times 4 = 12$ $4 + 4 + 4 = 12$ |
| Numberlines to show repeated groups | Using a beadstring 3×4  | Represent this pictorially alongside a number line e.g.  | Abstract number line showing three jumps of four  |
| Doubling | Using Numicon with part-whole model  | Using dots with part-whole model  | Using numbers with part-whole model  |

| | CONCRETE | PICTORIAL | ABSTRACT |
|---|---|---|---|
| Using arrays to illustrate commutativity | <p>Counters and other objects can also be used.</p> $2 \times 5 = 5 \times 2$  <p>2 lots of 5 5 lots of 2</p> | <p>Children to represent the arrays pictorially.</p>  | <p>Children to be able to use an array to write a range of calculations.</p> $10 = 2 \times 5$ $5 \times 2 = 10$ $2 + 2 + 2 + 2 + 2 = 10$ $10 = 5 + 5$ |

YEAR 2 – MULTIPLICATION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|---|--|
| repeated addition grouping equal groups of double multiply times lots of array | The whole is _____ there are _____ equal parts of _____ (The whole is 24 there are 4 equal parts of 6) |

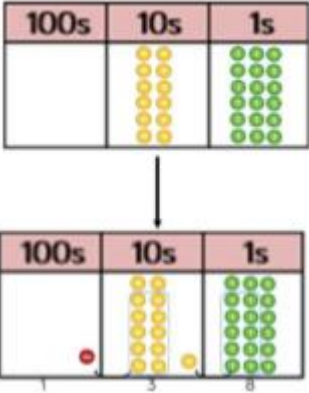
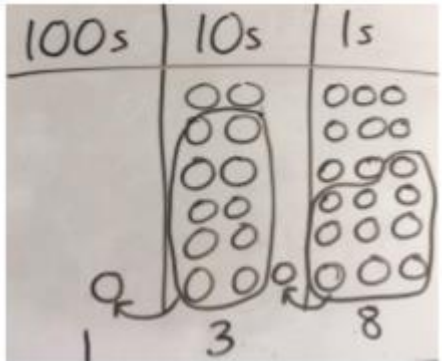
YEAR 3 – MULTIPLICATION

| | CONCRETE | PICTORIAL | ABSTRACT |
|--|---|--|---|
| Partition to multiply (moving to formal method) | With place value counters 3×23  | Children to represent the counters pictorially  | Using grid method moving onto formal method.  |

YEAR 3 – MULTIPLICATION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|--|--|
| repeated addition multiply times <i>grid method</i> grouping lots of <i>product</i> equal groups of array <i>short multiplication</i> double <i>partitioning</i> | The whole is _____ there are _____ equal parts of _____ (The whole is 24 there are 4 equal parts of 6) The product is _____ there are _____ equal groups of _____ (The product is 24 there are 4 equal groups of 6) |

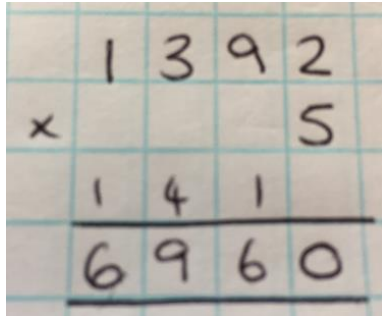
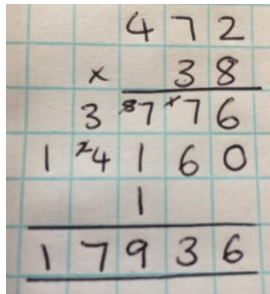
YEAR 4 – MULTIPLICATION

| | CONCRETE | PICTORIAL | ABSTRACT | | | | | | | | | | | | | | | | |
|---|--|--|--|--|----------|----------|----------|----------|--|--|----------|----------|----------|----------|--|----------|----------|----------|----------|
| <p>Formal column method (including exchanging)</p> <p>TO x O HTO x O</p> | <p>With place value counters</p>  | <p>Children to represent the counters pictorially</p>  | <p>Using formal method.</p> <table border="1" style="width: 100%; text-align: center; border-collapse: collapse;"> <tr> <td style="width: 25%;"></td> <td style="width: 25%;">2</td> <td style="width: 25%;">3</td> <td style="width: 25%;">5</td> </tr> <tr> <td>x</td> <td></td> <td></td> <td>6</td> </tr> <tr> <td>1</td> <td>2</td> <td>3</td> <td></td> </tr> <tr style="border-top: 2px solid black;"> <td>1</td> <td>4</td> <td>1</td> <td>0</td> </tr> </table> | | 2 | 3 | 5 | x | | | 6 | 1 | 2 | 3 | | 1 | 4 | 1 | 0 |
| | 2 | 3 | 5 | | | | | | | | | | | | | | | | |
| x | | | 6 | | | | | | | | | | | | | | | | |
| 1 | 2 | 3 | | | | | | | | | | | | | | | | | |
| 1 | 4 | 1 | 0 | | | | | | | | | | | | | | | | |

YEAR 4 – MULTIPLICATION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|---|---|
| <p>repeated addition</p> <p>multiply times</p> <p>grid method</p> <p>exchange</p> <p>grouping</p> <p>lots of</p> <p>product</p> <p>equal groups of</p> <p>array</p> <p>short multiplication</p> <p>double partitioning</p> <p>column</p> | <p>The whole is _____ there are _____ equal parts of _____ (The whole is 24 there are 4 equal parts of 6)</p> <p>The product is _____ there are _____ equal groups of _____ (The product is 24 there are 4 equal groups of 6)</p> |

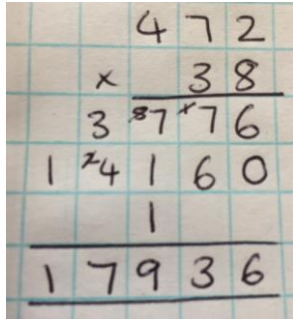
YEAR 5 – MULTIPLICATION

| | CONCRETE | PICTORIAL | ABSTRACT |
|--|---|-----------|---|
| Short multiplication ThHTO x O | | | Using formal method.  |
| Long multiplication ThHTO x O | <i>When children start to multiply 3d x 3d and 4d x 2d etc., they should be confident with the abstract</i> | | Using formal method.  |

YEAR 5 – MULTIPLICATION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|---|--|
| repeated addition multiply times grid method exchange grouping lots of product equal groups of array short multiplication double partitioning column <i>long multiplication</i> | The whole is _____ there are _____ equal parts of _____ (The whole is 24 there are 4 equal parts of 6) The product is _____ there are _____ equal groups of _____ (The product is 24 there are 4 equal groups of 6) |

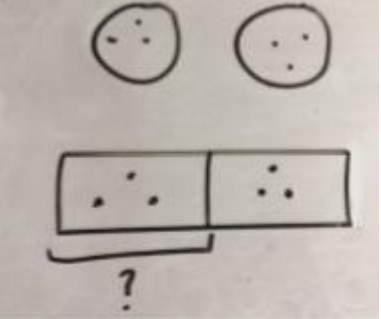
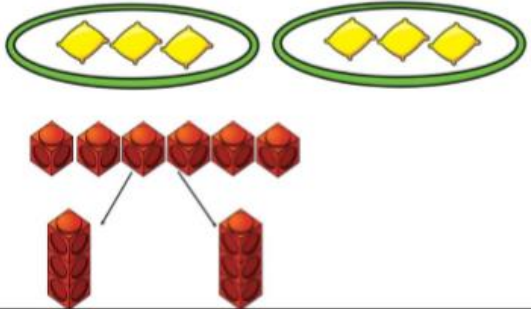


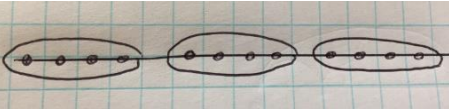
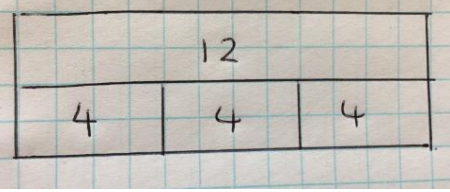
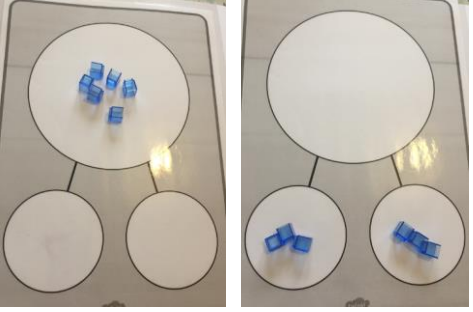
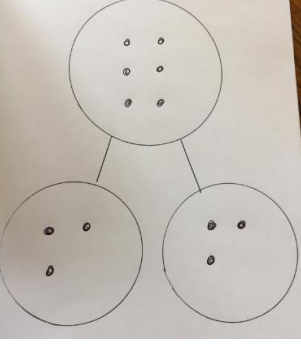
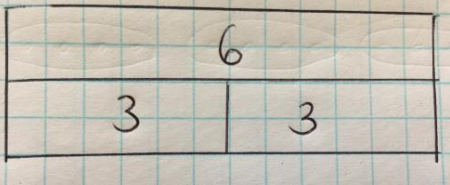
YEAR 6 – MULTIPLICATION

| | CONCRETE | PICTORIAL | ABSTRACT |
|--|----------|-----------|--|
| Long multiplication ThHTO x O | | | Using formal method.  |
| Using known number facts | | | $7 \times 3 = 21$ $0.7 \times 3 = 2.1$ $0.7 \times 0.3 = 0.21$ $70 \times 3 = 210$ $70 \times 30 = 2100$ |

YEAR 6 – MULTIPLICATION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|---|--|
| repeated addition multiply times grid method exchange grouping lots of product equal groups of array short multiplication long multiplication double partitioning column | The whole is _____ there are _____ equal parts of _____ (The whole is 24 there are 4 equal parts of 6) The product is _____ there are _____ equal groups of _____ (The product is 24 there are 4 equal groups of 6) |


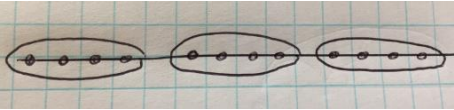
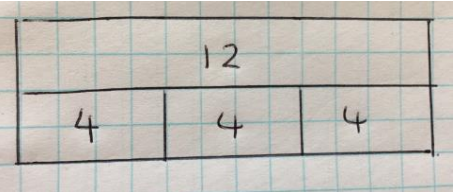
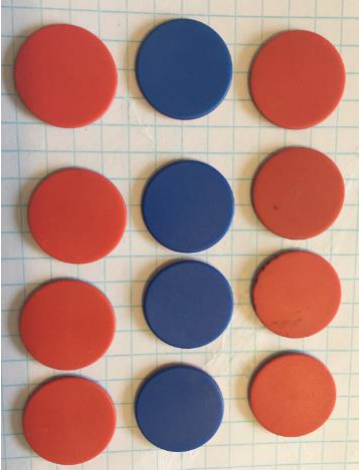
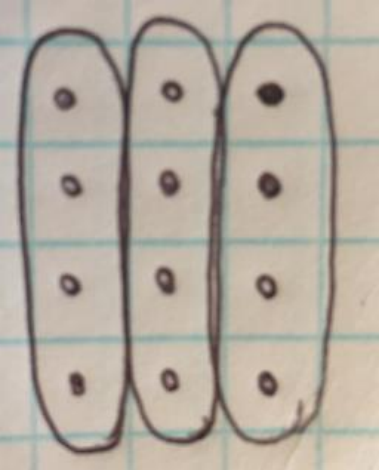
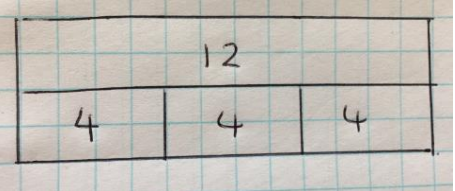

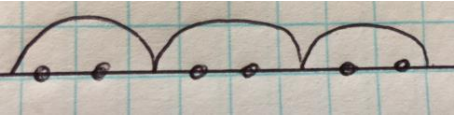
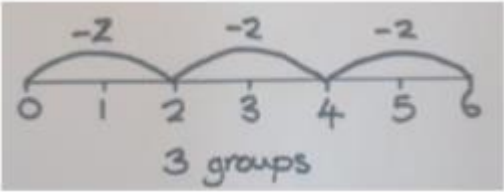
YEAR 1 –DIVISION

| | CONCRETE | PICTORIAL | ABSTRACT |
|-------------------------------|---|---|--|
| Sharing | <p>Using a range of objects</p> $6 \div 2$ | <p>Represent the sharing pictorially</p>  | <p>Using bar model</p> $6 \div 2 = 3$ |
| |  | |  <p>Children should also be encouraged to use their 2 times tables facts.</p> |
| Grouping | <p>Using a beadstring</p>  | <p>Represent the bead string pictorially</p>  | <p>Using bar model</p>  |
| Halving of even number | <p>Using cubes</p>  | <p>Represent the halving pictorially</p>  | <p>Using bar model</p>  |

YEAR 1 - DIVISION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|---|--|
| <div style="display: flex; justify-content: space-around;"> <i>sharing</i> <i>divide</i> <i>grouping</i> <i>half</i> </div> <p><i>halving</i></p> | <p><i>The whole is _____ there are _____ equal parts of _____ (The whole is 24 there are 4 equal parts of 6)</i></p> |



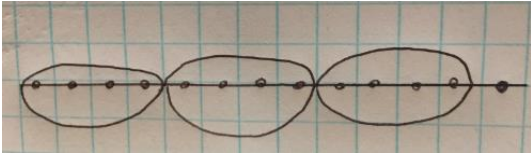
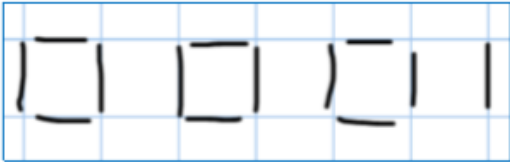
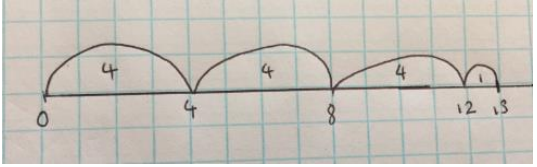
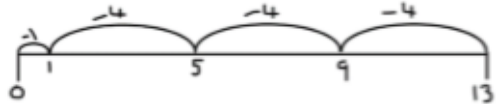
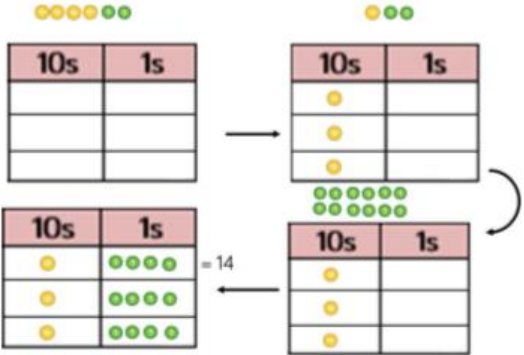
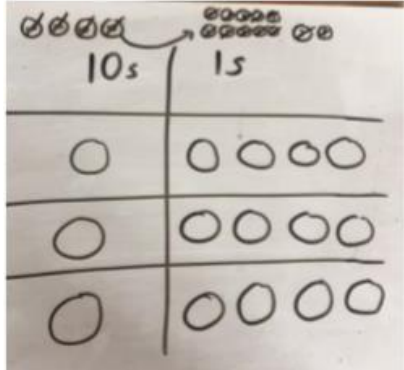
YEAR 2 –DIVISION

| | CONCRETE | PICTORIAL | ABSTRACT |
|--|--|---|--|
| Grouping <i>*Same as Y1*</i> | Using a bead string  | Represent the bead string pictorially  | Using bar model  |
| Arrays | Using cubes or counters  | Represent the array pictorially  | Using bar model  |
| Repeated subtraction | Using a bead string  | Children to represent the bead string pictorially  | Abstract number line to represent the equal groups that have been subtracted.  |

YEAR 2 - DIVISION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|--|---|
| <div style="display: flex; justify-content: space-between;"> sharing divide grouping half </div> <div style="display: flex; justify-content: space-between; margin-top: 5px;"> halving arrays repeated subtraction </div> | <p>The whole is _____ there are _____ equal parts of _____ (The whole is 24 there are 4 equal parts of 6)</p> |

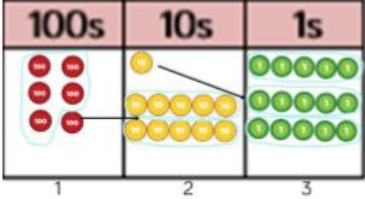
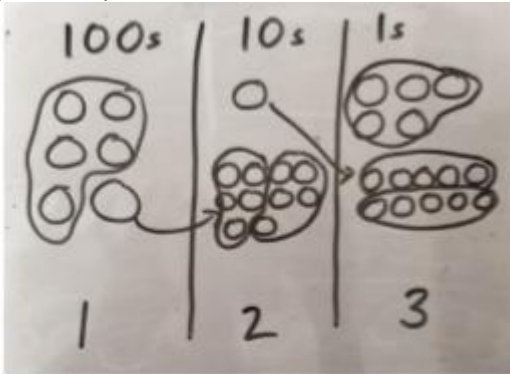
YEAR 3 –DIVISION

| | CONCRETE | PICTORIAL | ABSTRACT |
|------------------------------------|---|---|---|
| <p>TO÷O with remainders</p> | <p>Using a bead string</p>  <p>Using lollipop sticks.</p> $13 \div 4$ <p>Use of lollipop sticks to form wholes- squares are made because we are dividing by 4.</p>  <p>There are 3 whole squares, with 1 left over.</p> | <p>Represent the bead string pictorially</p>  <p>Represent the lollipop sticks pictorially</p>  <p>There are 3 whole squares, with 1 left over.</p> | <p>Using number line</p> $13 \div 4 = 3 \text{ remainder } 1$ <p>Children should be encouraged to use their times table facts; they could also represent repeated addition on a number line.</p> <p>'3 groups of 4, with 1 left over'</p> <p><u>Times tables Facts</u></p>  <p><u>Repeated Subtraction</u></p>  |
| <p>Sharing</p> | <p>Using place value counters</p> $42 \div 3 = 14$  | <p>Children to represent the place value pictorially</p>  | <p>Write calculation to show steps</p> $42 \div 3$ $42 = 30 + 12$ $30 \div 3 = 10$ $12 \div 3 = 4$ $10 + 4 = 14$ |

YEAR 3 - DIVISION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|--|---|
| <div style="display: flex; justify-content: space-between;"> <div style="width: 45%;"> <p>sharing halving</p> <p>arrays</p> </div> <div style="width: 45%;"> <p>divide repeated subtraction</p> <p>grouping remainders</p> </div> </div> <p style="text-align: right; margin-top: 10px;">half</p> | <p>The whole is _____ there are _____ equal parts of _____ (The whole is 24 there are 4 equal parts of 6)</p> <p><i>The whole is _____ there are _____ equal parts of _____ and _____ remainders (The whole is 26 there are 4 equal parts of 6 and 2 remainders)</i></p> |

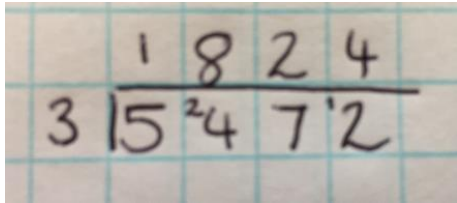
YEAR 4 –DIVISION

| | CONCRETE | PICTORIAL | ABSTRACT |
|-----------------------|--|---|---|
| Short division | <p>Using place value counters to group. $615 \div 5$</p>  <ol style="list-style-type: none"> 1. Make 615 with place value counters. 2. How many groups of 5 hundreds can you make with 6 hundred counters? 3. Exchange 1 hundred for 10 tens. 4. How many groups of 5 tens can you make with 11 ten counters? 5. Exchange 1 ten for 10 ones. 6. How many groups of 5 ones can you make with 15 ones? | <p>Represent the place value counters pictorially.</p>  | <p>Use the short division scaffold to calculate</p> $ \begin{array}{r} 123 \\ 5 \overline{) 615} \\ \underline{5} \\ 11 \\ \underline{10} \\ 15 \\ \underline{15} \\ 0 \end{array} $ |

YEAR 4 - DIVISION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|--|---|
| <p style="text-align: center;">sharing divide grouping half</p> <p>halving arrays repeated subtraction remainders short division</p> <p>bus shelter</p> | <p>The whole is _____ there are _____ equal parts of _____ (The whole is 24 there are 4 equal parts of 6)</p> <p>The whole is _____ there are _____ equal parts of _____ and _____ remainders (The whole is 26 there are 4 equal parts of 6 and 2 remainders)</p> |

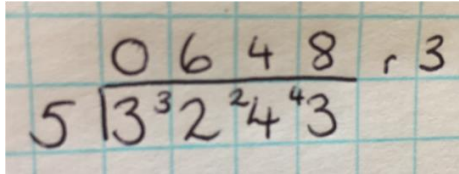
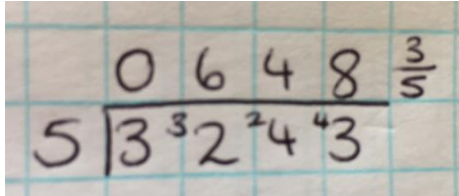
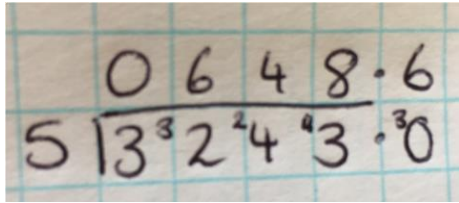
YEAR 5 –DIVISION


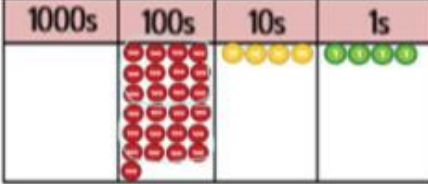
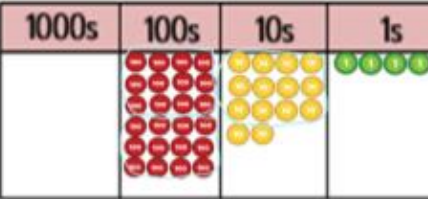
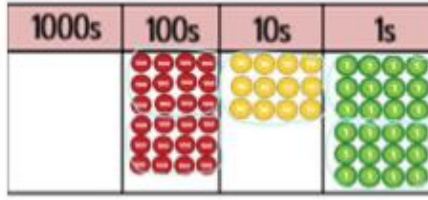
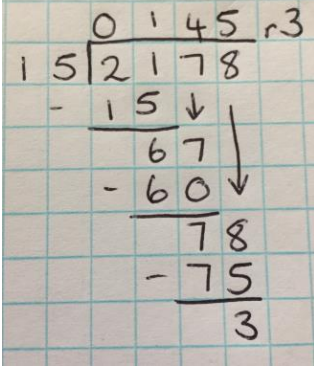
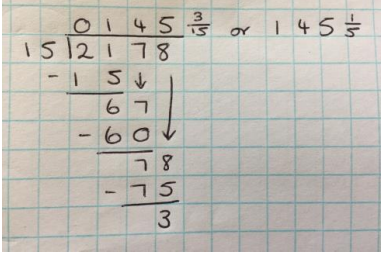
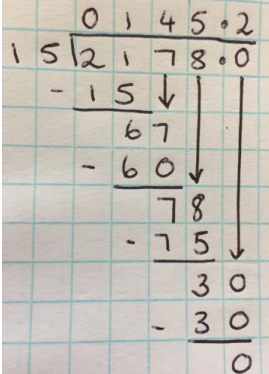
| | CONCRETE | PICTORIAL | ABSTRACT |
|--|----------|-----------|--|
| Short division Up to ThHTO ÷O | | | Using formal method  |

YEAR 5 - DIVISION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|---|--|
| sharing divide grouping half halving arrays repeated subtraction remainders short division bus shelter | The whole is _____ there are _____ equal parts of _____ (The whole is 24 there are 4 equal parts of 6) The whole is _____ there are _____ equal parts of _____ and _____ remainders (The whole is 26 there are 4 equal parts of 6 and 2 remainders) <i>The quotient of _____ and _____ is _____ (The quotient of 24 and 6 is 4)</i> |

YEAR 6 –DIVISION

| | CONCRETE | PICTORIAL | ABSTRACT |
|---|----------|-----------|---|
| <p>Short division</p> <p>Interpret remainders as whole numbers, fractions or decimals</p> | | | <p>Using formal method</p> <p><u>Whole Number Remainder</u></p>  <p><u>Fraction Remainder</u></p>  <p><u>Decimal Remainder</u></p>  |

| | CONCRETE | PICTORIAL | ABSTRACT |
|--|---|--|--|
| <p>Long division</p> <p>Interpret remainders as whole numbers, fractions or decimals</p> | <p>2544 ÷ 12</p>  <p>We can't group 2 thousands into groups of 12 so will exchange them.</p>  <p>We can group 24 hundreds into groups of 12 which leaves with 1 hundred.</p>  <p>After exchanging the hundred, we have 14 tens. We can group 12 tens into a group of 12, which leaves 2 tens.</p>  <p>After exchanging the 2 tens, we have 24 ones. We can group 24 ones into 2 group of 12, which leaves no remainder.</p> | $12 \overline{) 2544}$ $\begin{array}{r} 02 \\ \underline{24} \\ 1 \end{array}$ $12 \overline{) 2544}$ $\begin{array}{r} 021 \\ \underline{24} \\ 14 \\ \underline{12} \\ 2 \end{array}$ $12 \overline{) 2544}$ $\begin{array}{r} 0212 \\ \underline{24} \\ 14 \\ \underline{12} \\ 24 \\ \underline{24} \\ 0 \end{array}$ | <p>Using formal method</p> <p>Whole Number Remainder</p>  <p>Fractional Remainder</p>  <p>Decimal Remainder</p>  |

YEAR 6 - DIVISION

| VOCABULARY <i>(new vocab in bold/italic)</i> | STEM SENTENCES <i>(new vocab in bold/italic)</i> |
|---|---|
| <div style="display: flex; flex-wrap: wrap; justify-content: space-between;"> <div style="width: 20%;">sharing</div> <div style="width: 20%;">divide</div> <div style="width: 20%;">grouping</div> <div style="width: 20%;">half</div> </div> <div style="display: flex; flex-wrap: wrap; justify-content: space-between; margin-top: 5px;"> <div style="width: 20%;">halving</div> <div style="width: 20%;">arrays</div> <div style="width: 20%;">repeated subtraction</div> <div style="width: 20%;">remainders</div> <div style="width: 20%;">short division</div> </div> <div style="margin-top: 5px;"> bus shelter <i>long division</i> </div> | <p>The whole is _____ there are _____ equal parts of _____ (The whole is 24 there are 4 equal parts of 6)</p> <p>The whole is _____ there are _____ equal parts of _____ and _____ remainders (The whole is 26 there are 4 equal parts of 6 and 2 remainders)</p> <p>The quotient of _____ and _____ is _____ (The quotient of 24 and 6 is 4)</p> |